

OXFORD CAMBRIDGE AND RSA EXAMINATIONS

**Advanced Subsidiary General Certificate of Education
Advanced General Certificate of Education**

MATHEMATICS

4722

Core Mathematics 2

Monday

16 JANUARY 2006

Morning

1 hour 30 minutes

Additional materials:

8 page answer booklet

Graph paper

List of Formulae (MF1)

TIME 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are permitted to use a graphical calculator in this paper.

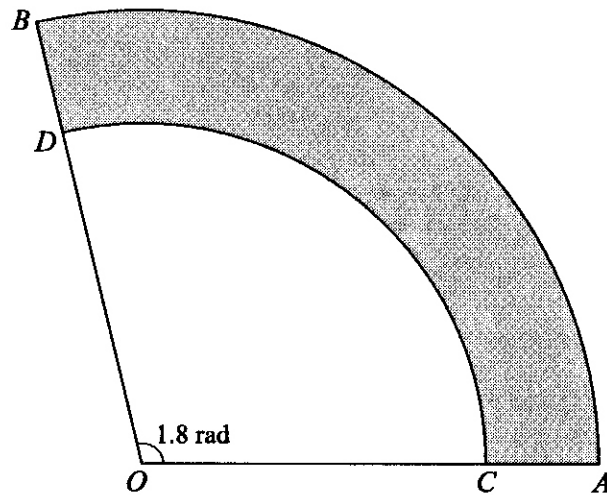
INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.
- Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
- **You are reminded of the need for clear presentation in your answers.**

This question paper consists of 4 printed pages.

- 1 The 20th term of an arithmetic progression is 10 and the 50th term is 70.
- (i) Find the first term and the common difference. [4]
- (ii) Show that the sum of the first 29 terms is zero. [2]
- 2 Triangle ABC has $AB = 10$ cm, $BC = 7$ cm and angle $B = 80^\circ$. Calculate
- (i) the area of the triangle, [2]
- (ii) the length of CA , [2]
- (iii) the size of angle C . [2]
- 3 (i) Find the first three terms of the expansion, in ascending powers of x , of $(1 - 2x)^{12}$. [3]
- (ii) Hence find the coefficient of x^2 in the expansion of
- $$(1 + 3x)(1 - 2x)^{12}. \quad [3]$$

4



The diagram shows a sector OAB of a circle with centre O . The angle AOB is 1.8 radians. The points C and D lie on OA and OB respectively. It is given that $OA = OB = 20$ cm and $OC = OD = 15$ cm. The shaded region is bounded by the arcs AB and CD and by the lines CA and DB .

- (i) Find the perimeter of the shaded region. [3]
- (ii) Find the area of the shaded region. [3]

5 In a geometric progression, the first term is 5 and the second term is 4.8.

(i) Show that the sum to infinity is 125. [2]

(ii) The sum of the first n terms is greater than 124. Show that

$$0.96^n < 0.008,$$

and use logarithms to calculate the smallest possible value of n . [6]

6 (a) Find $\int (x^{\frac{1}{2}} + 4) dx$. [4]

(b) (i) Find the value, in terms of a , of $\int_1^a 4x^{-2} dx$, where a is a constant greater than 1. [3]

(ii) Deduce the value of $\int_1^{\infty} 4x^{-2} dx$. [1]

7 (i) Express each of the following in terms of $\log_{10} x$ and $\log_{10} y$.

(a) $\log_{10} \left(\frac{x}{y} \right)$ [1]

(b) $\log_{10} (10x^2y)$ [3]

(ii) Given that

$$2 \log_{10} \left(\frac{x}{y} \right) = 1 + \log_{10} (10x^2y),$$

find the value of y correct to 3 decimal places. [4]

8 The cubic polynomial $2x^3 + kx^2 - x + 6$ is denoted by $f(x)$. It is given that $(x + 1)$ is a factor of $f(x)$.

(i) Show that $k = -5$, and factorise $f(x)$ completely. [6]

(ii) Find $\int_{-1}^2 f(x) dx$. [4]

(iii) Explain with the aid of a sketch why the answer to part (ii) does not give the area of the region between the curve $y = f(x)$ and the x -axis for $-1 \leq x \leq 2$. [2]

[Question 9 is printed overleaf.]

- 9 (i) Sketch, on a single diagram showing values of x from -180° to $+180^\circ$, the graphs of $y = \tan x$ and $y = 4 \cos x$. [3]

The equation

$$\tan x = 4 \cos x$$

has two roots in the interval $-180^\circ \leq x \leq 180^\circ$. These are denoted by α and β , where $\alpha < \beta$.

- (ii) Show α and β on your sketch, and express β in terms of α . [3]

- (iii) Show that the equation $\tan x = 4 \cos x$ may be written as

$$4 \sin^2 x + \sin x - 4 = 0.$$

Hence find the value of $\beta - \alpha$, correct to the nearest degree. [6]